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# Using Multiagent Negotiation to Model Water Resources Systems Operations

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# Management of Water Resources Systems

- The operations of water resources infrastructures, like dams and diversions, involve multiple conflicting interests and stakeholders
- Centralized approaches [Zeitoun and Warner, *Water Policy*, 2006]
  - Full knowledge
  - Perfect application of the generated policies
- Agent-based approaches [Giuliani et al., *J Water Res Pl-ASCE*, 2015; Yang et al., *Water Resour Res*, 2009]

## **Agent = stakeholder**

- Distributed Constraint Processing [Amigoni et al., *AAMAS*, 2015]
- Negotiation [Adams et al., *J Econ Behav Organ*, 1996; Thoyer et al., *JASSS-J Artif Soc S*, 2001]
  - Agents have full knowledge of the preferences of other agents



## Purpose

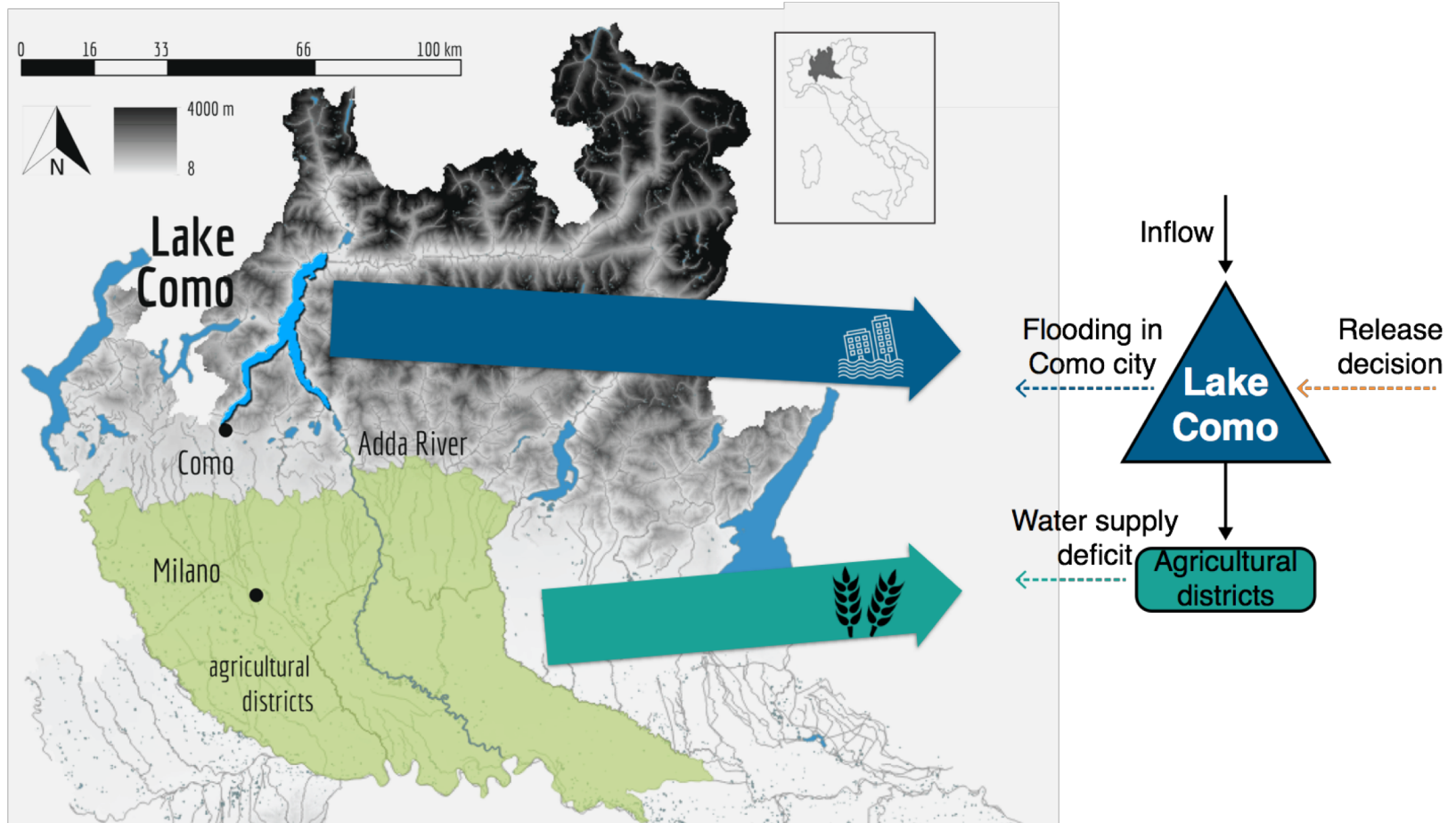
We propose a model based on a general **monotonic concession negotiation** framework that allows the stakeholders-agents of a regulated lake to periodically reach agreements on the lake operating policy that determines the amount of water to release daily

No need for agents to know all their preferences



# Case study

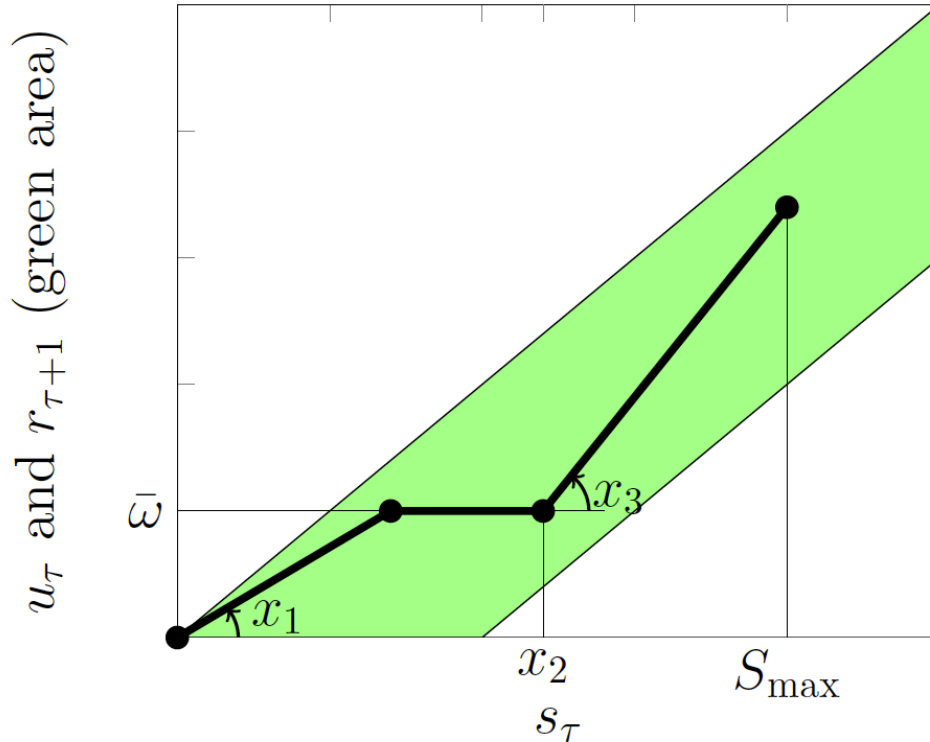
## Lake Como system, in Northern Italy





## Case study: release policy

The water release at day  $\tau$ ,  $r_\tau$ , is controlled using the *standard operating policy* [Draper and Lund, *J Water Res Pl-ASCE*, 2004] according to the volume of water stored in the reservoir  $s_\tau$



Feasibility region (green)

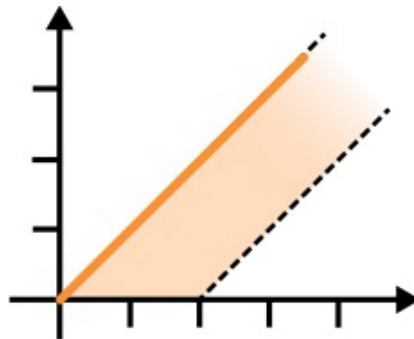
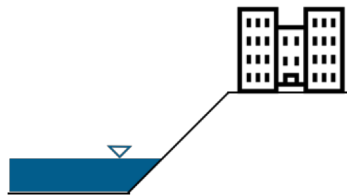
The shape of the policy depends on  $x_1, x_2, x_3$



# Case study: agents-stakeholders

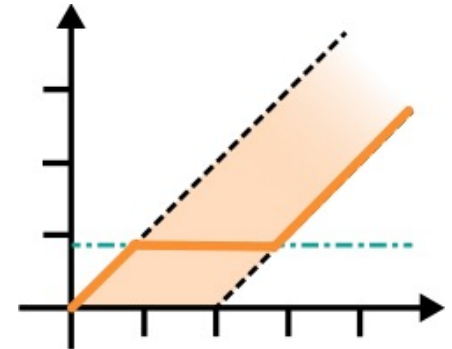
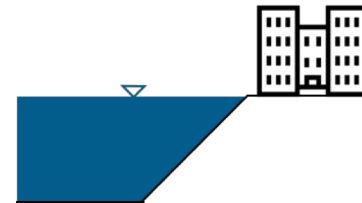
**city agent:** communities living on the lake shores, who are worried about floods

Its cost function prefers **low** water levels



**irr agent:** farmers in the downstream irrigation districts, who need constant water supply  $\bar{\omega}$  to grow crops

Its cost function prefers **high** water levels



Agents then negotiate on  $x_1, x_2, x_3$



# Negotiation

A negotiation is performed for a block  $B_j$  of  $b$  days

We consider a monotonic concession protocol with a mediator

Negotiation develops in steps  $0, 1, \dots, t, \dots$

At step 0, agents calculate their best proposals  $p_i^0$  and send them to the mediator

At each step  $t$ :

1. The mediator calculates the current agreement  $a^t = \mathcal{A}(\{p_1^t, p_2^t, \dots, p_n^t\})$  and send it to the agents
2. Agents calculate their proposals  $p_i^{t+1} = \mathcal{F}_i(p_i^t, a^t)$  and send them to the mediator



# Point-based protocol

[Amigoni and Gatti, *Auton Agent Multi-Ag*, 2007]

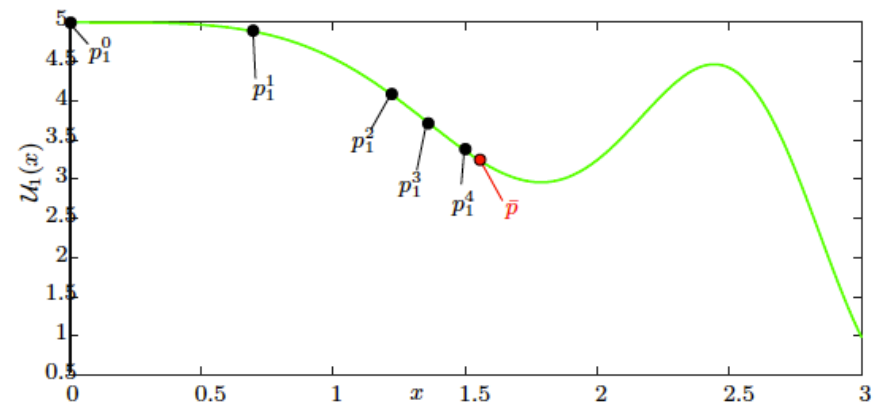
A proposal is a **vector of values**  
 $p_i^t = [x_1, x_2, x_3]$ , namely the  
release policy that agent  $i$  would  
like to adopt at step  $t$

$$p_i^{t+1} = \mathcal{F}_i(p_i^t, a^t) = p_i^t + \alpha_i \cdot (a^t - p_i^t)$$

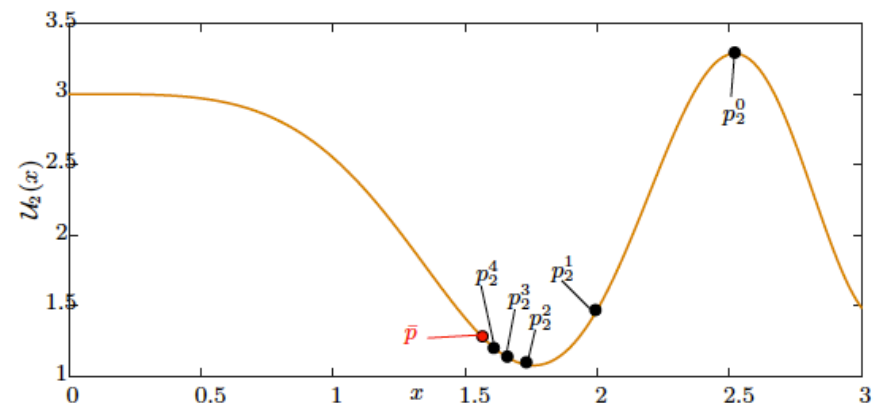
$\alpha_i \in [0,1]$ : concession  
coefficient of agent  $i$

$a^t$  is the average of proposals  $p_i^t$

Agreement:  $a^t = p_1^t = p_2^t = \dots = p_n^t$



(a) Utility function of agent 1 (and  $p_1^t$ )



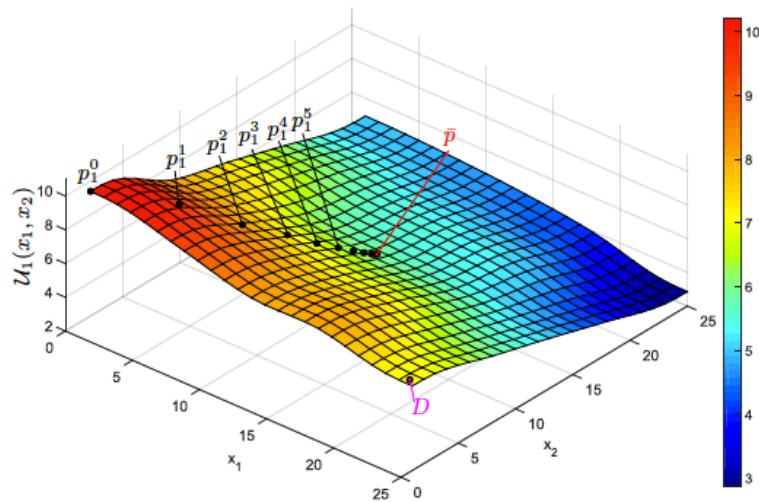
(b) Utility function of agent 2 (and  $p_2^t$ )



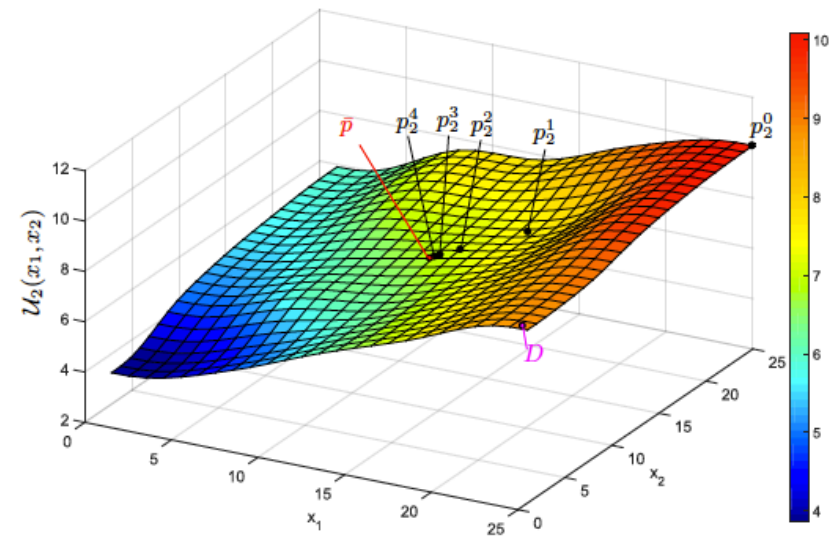
# Point-based protocol: properties

**Convergence** is guaranteed if all  $\alpha_i > 0$  (and the negotiation space is not empty)

**Pareto optimality** of the agreement is not guaranteed



(a) Utility function of agent 1 (and  $p_1^t$ )



(b) Utility function of agent 2 (and  $p_2^t$ )



## Set-based protocol

[Badica and Badica, *Proc. BCI*, 2012]

A proposal is a **set of vectors of values**  $p_i^t = \{[x_1, x_2, x_3]\}$ , namely the set of release policies that agent  $i$  could adopt at step  $t$

$$p_i^t = \mathcal{P}_i(\Gamma_i^t) = \{x \in \mathbb{R}^m \mid \mathcal{U}_i(x) \geq \Gamma_i^t\}$$

acceptable offers given the acceptability threshold  $\Gamma_i^t$

$$\Gamma_i^{t+1} = \Gamma_i^t - c_i$$

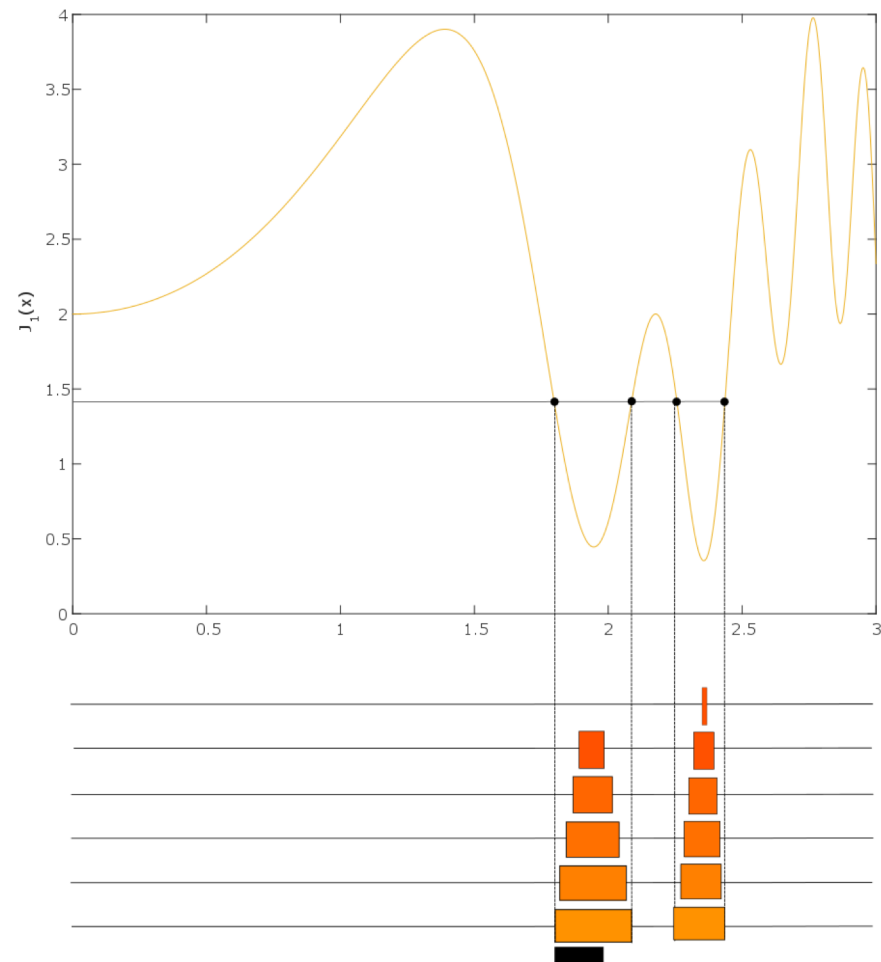
$c_i$ : concession  
step of agent  $i$

$$a^t = \bigcap_{i=1}^n p_i^t = \bigcap_{i=1}^n \mathcal{P}_i(\Gamma_i^t)$$

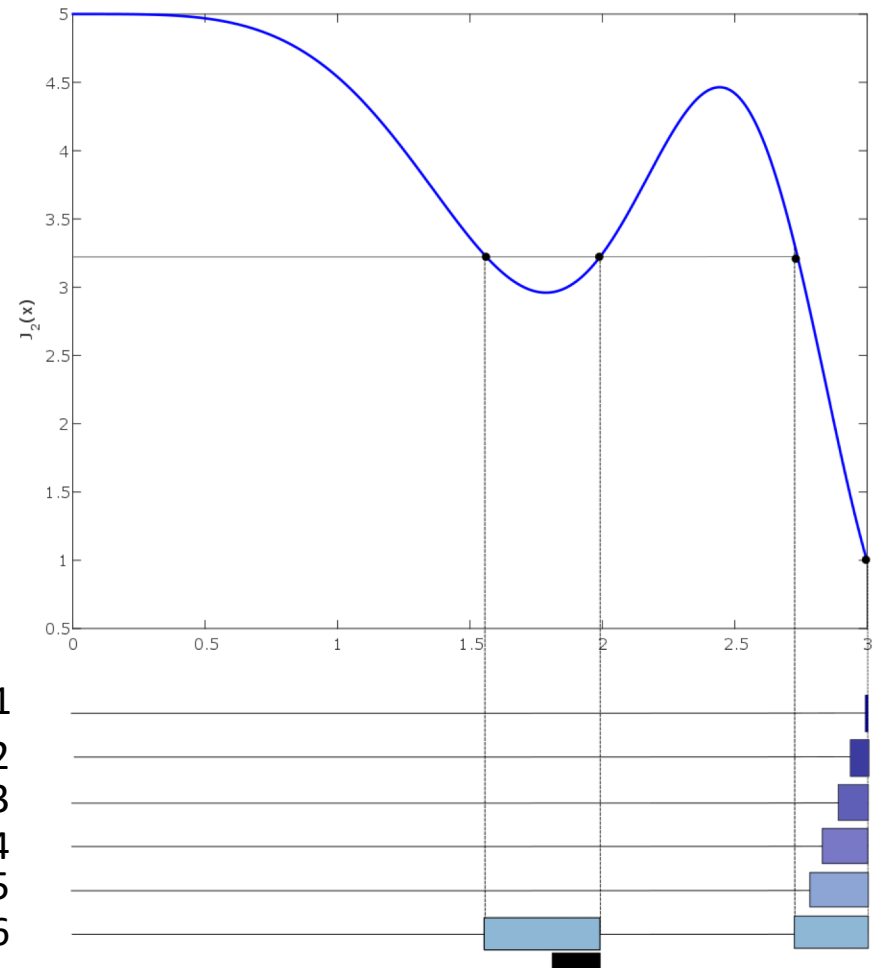
Agreement:  $a^t \neq \emptyset$



# Set-based protocol: example



t=1  
t=2  
t=3  
t=4  
t=5  
t=6



## Set-based protocol: properties

**Convergence** is guaranteed (if the negotiation space is not empty)

**Pareto optimality** of the agreement is guaranteed by construction

- with infinitely small  $c_i$ : the first agreement found is Pareto optimal
- with finite  $c_i$ : the first set of agreements found contains at least a Pareto optimal agreement





## Simulations

We generate inflow values  $q_\tau$  from a normal distribution  $\mathcal{N}(\mu_q, \sigma_q)$

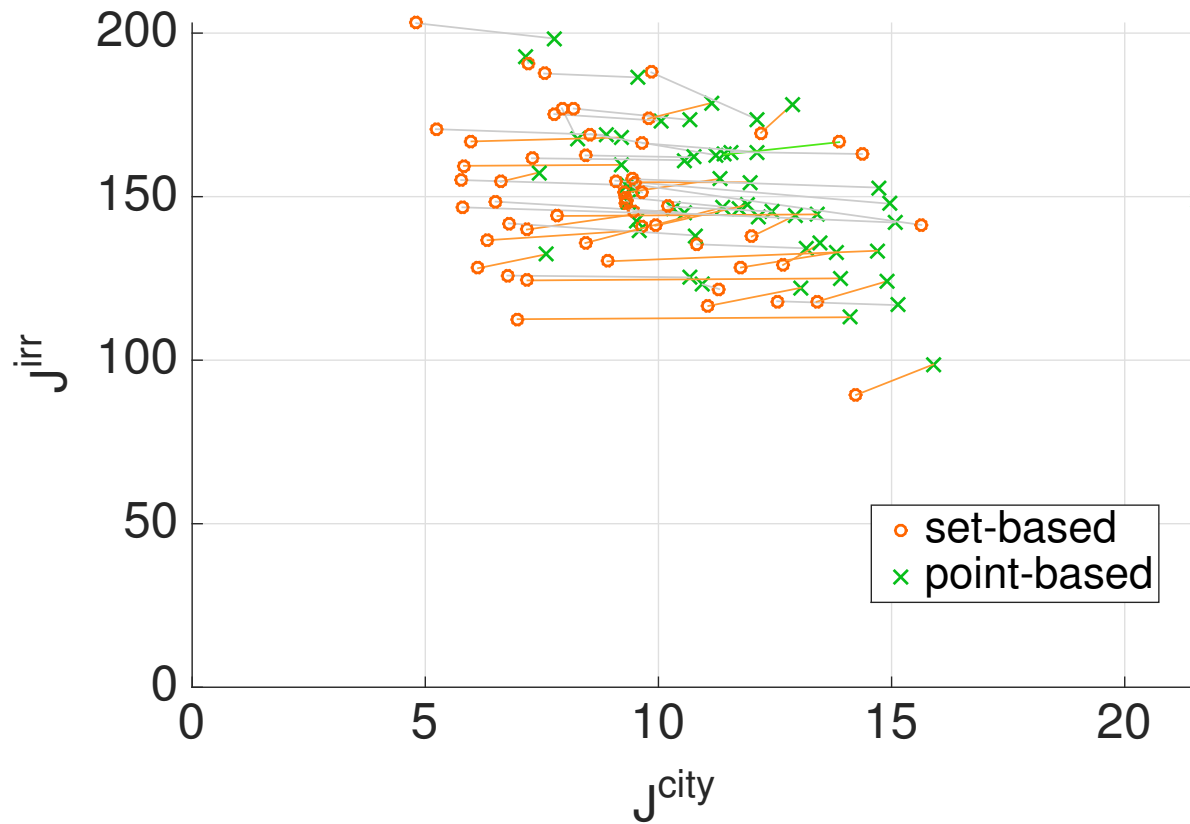
Data are synthetic but trigger realistic conflicts between floods and water demands, similar to those observed in real systems

A negotiation is performed for each block  $B_j$ , namely every  $b$  days

In negotiation for  $B_{j+1}$ , cost functions of the agents are calculated considering costs incurred by the agents over  $B_j$



## Simulations: point-based protocol vs. set-based protocol



Agreements relative to the same blocks  $B_j$

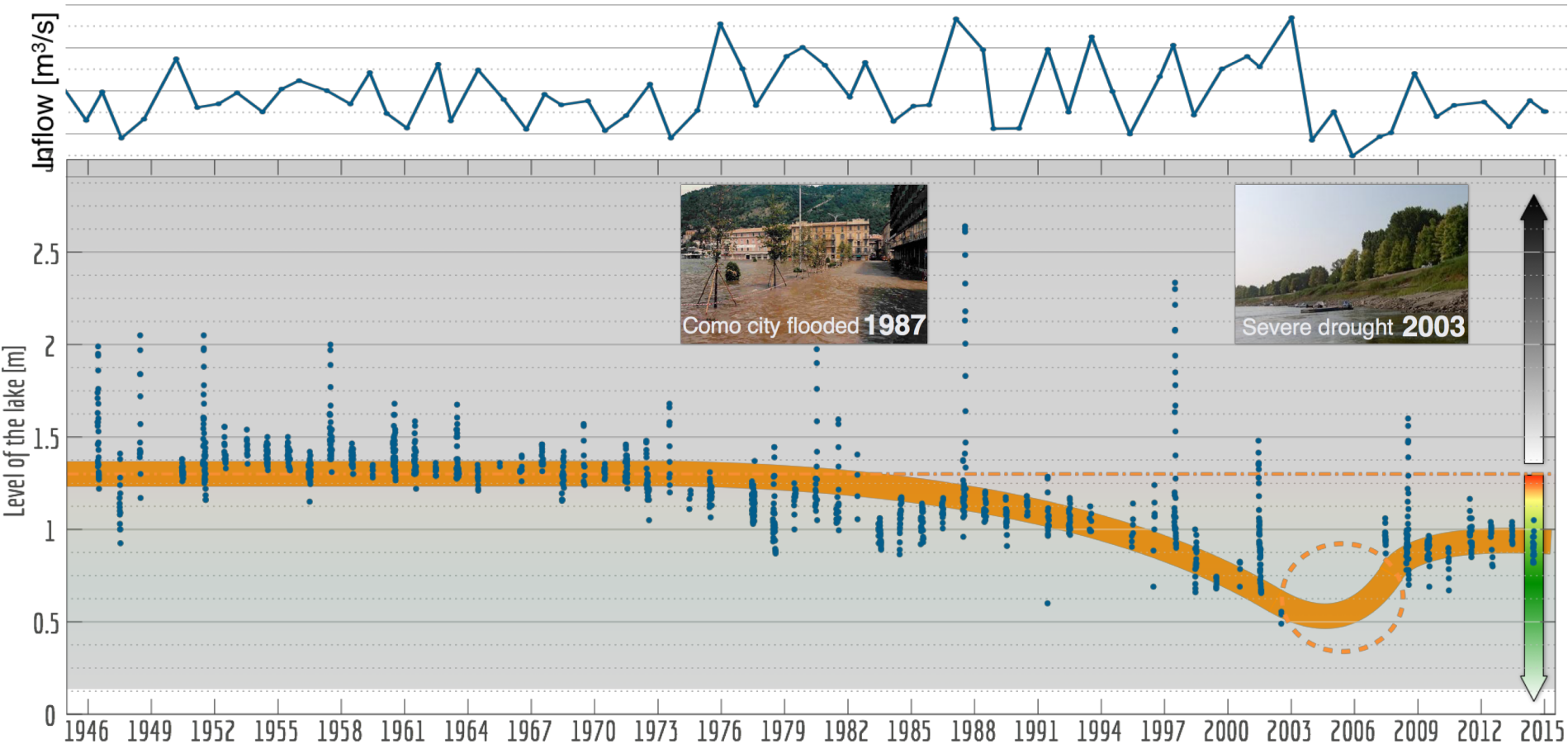
The color of the line segments shows the dominance



# Simulations: reproducing observed trends

## Observed data

Observed level of the Como lake 1946-2015, with a rather constant inflow



## Simulations: reproducing observed trends

### Model

The observed behavior of the lake regulator can be naturally captured in our model (set-based protocol) by setting the values of concession steps  $c_i$  according to the past performance of the agents

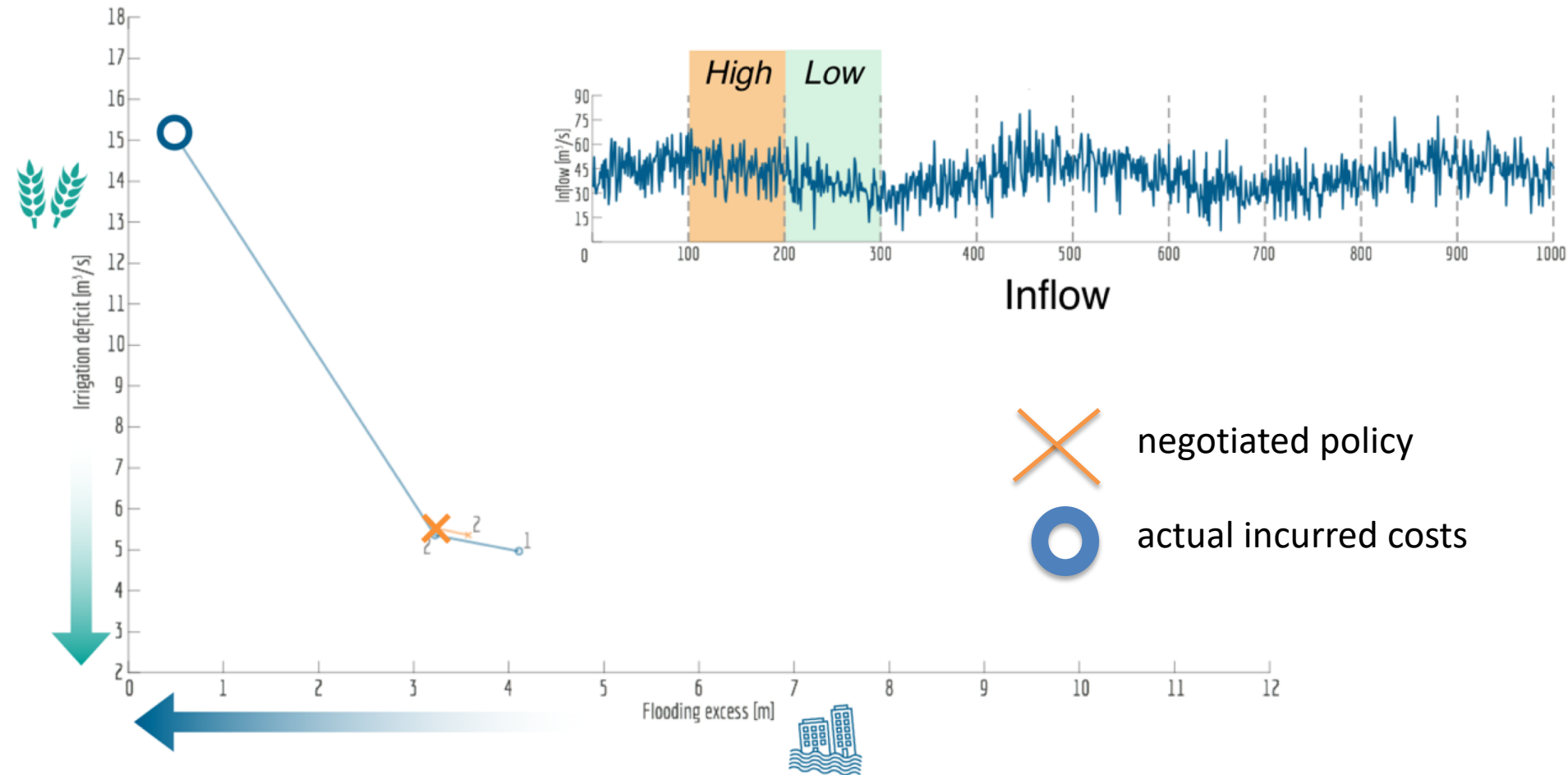
Informally, while negotiating the policy for block  $B_j$  agent  $i$  will use a concession step  $c_i$  which depends on the “satisfaction” of agent  $i$  in blocks  $B_{j-1}, B_{j-2}, \dots$

- If the city agent has recently experienced floods, its  $c_i$  will be small, namely the city agent will be rigid in conceding



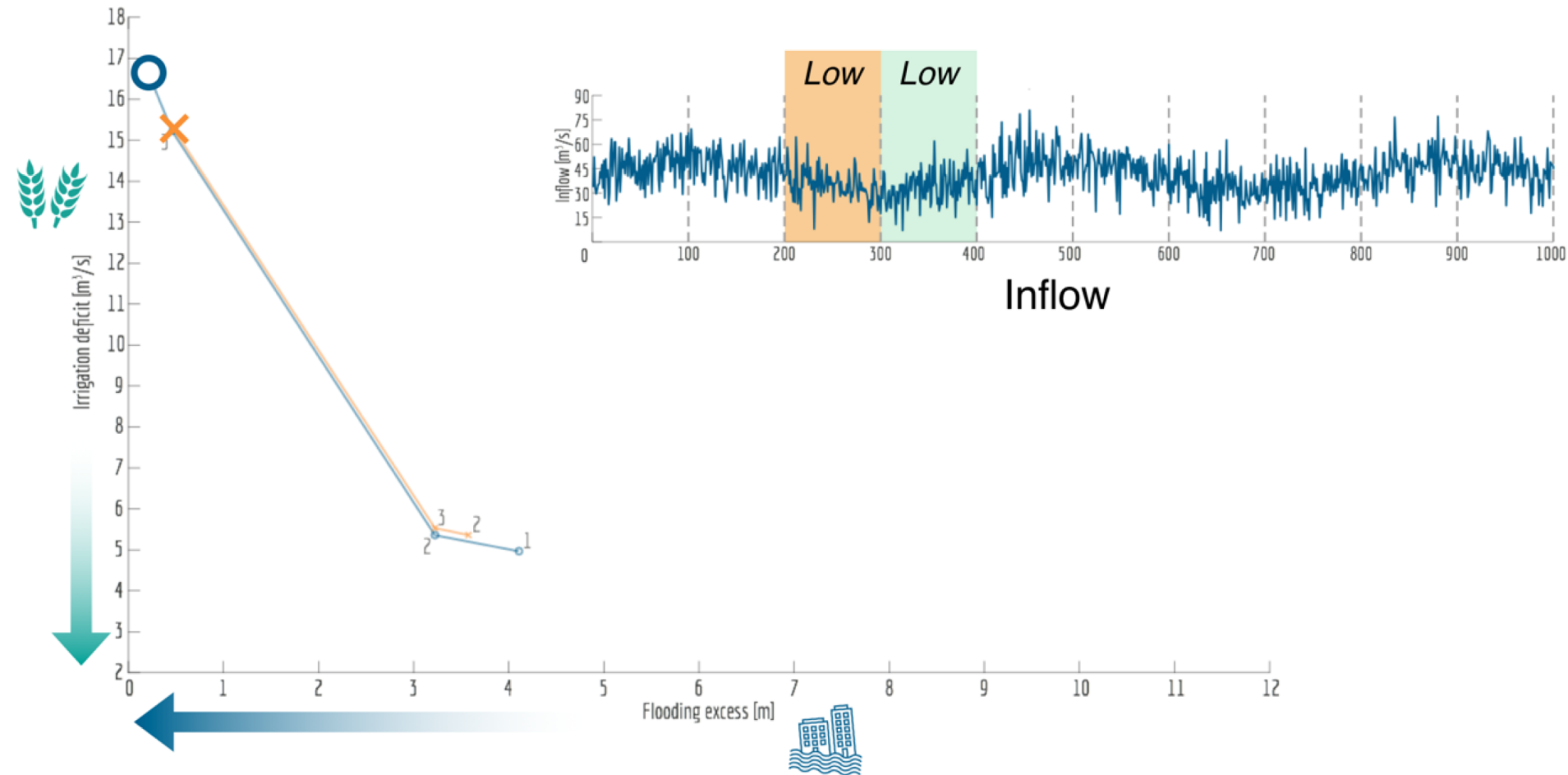
# Simulations: reproducing observed trends

## Drought occurrence



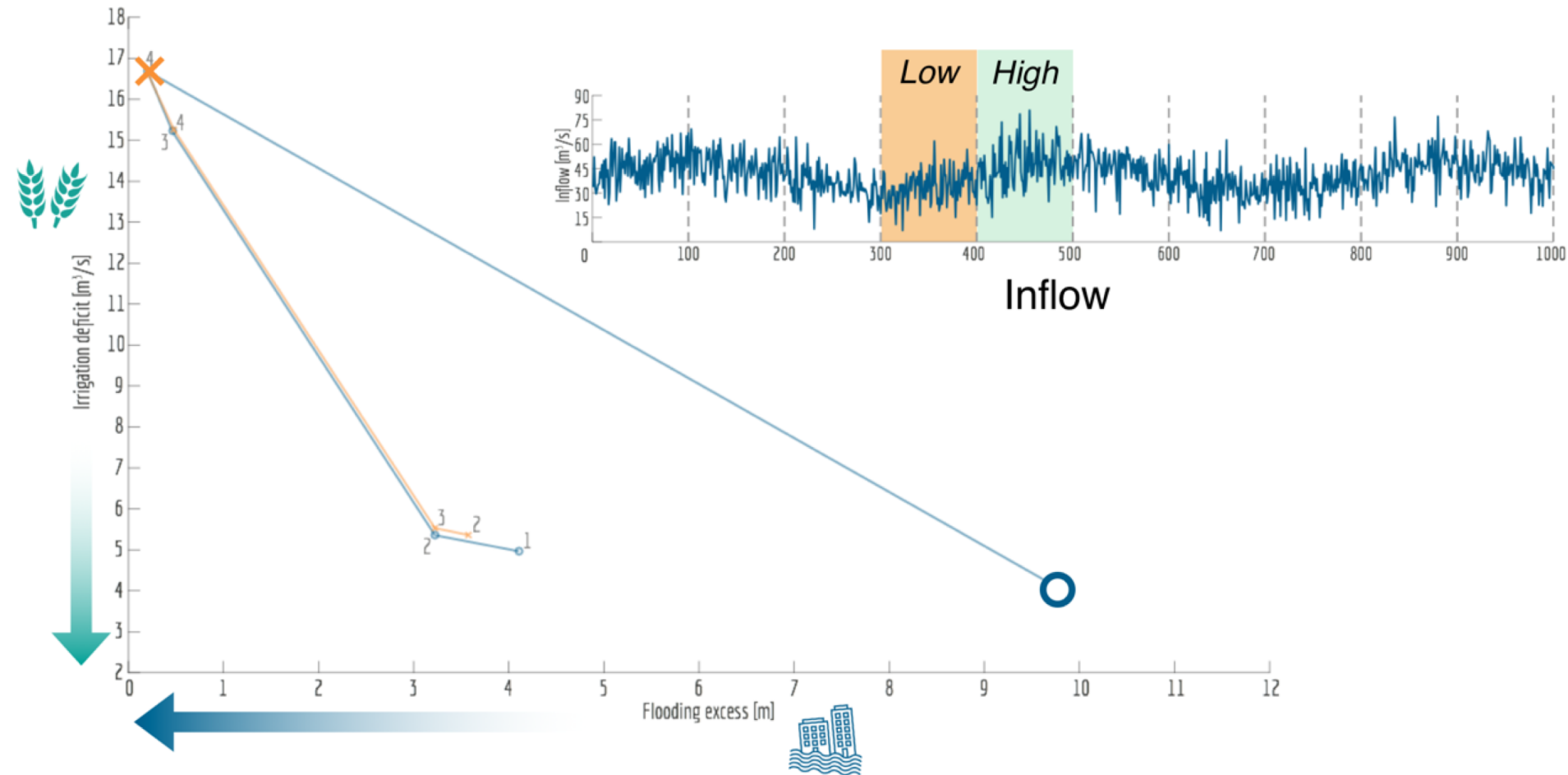
# Simulations: reproducing observed trends

## Drought reaction



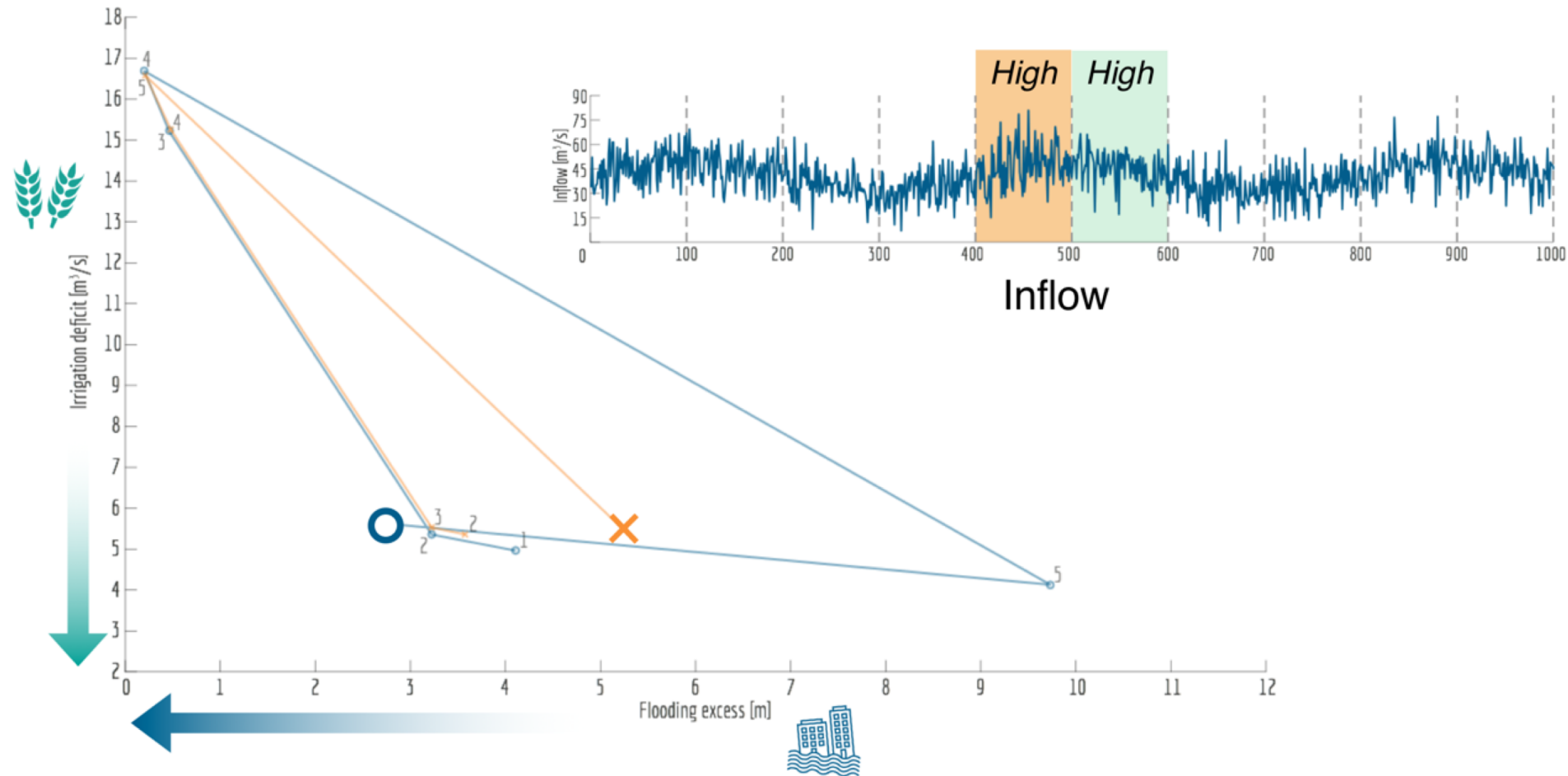
# Simulations: reproducing observed trends

## Flood occurrence



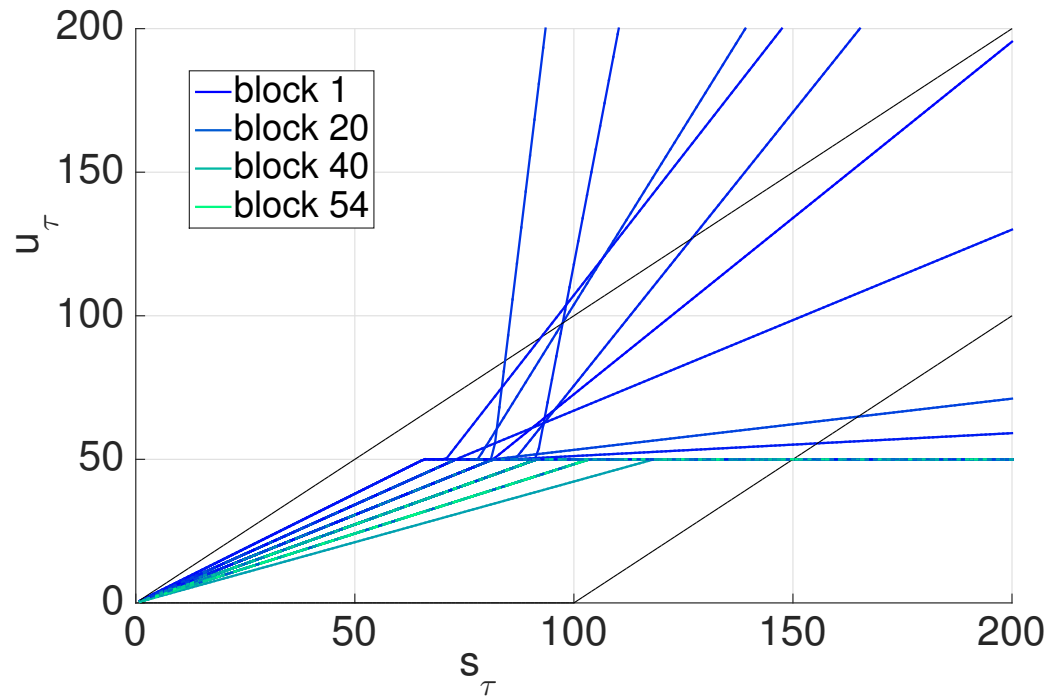
# Simulations: reproducing observed trends

## Flood reaction





## Simulations: decreasing inflow (1)

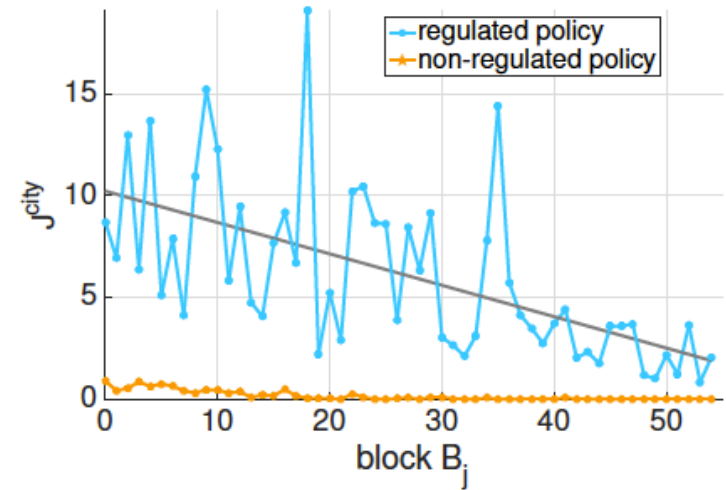


Release policies obtained with the set-based protocol for inflow  $q_\tau$  with a decreasing mean  $\mu_q$

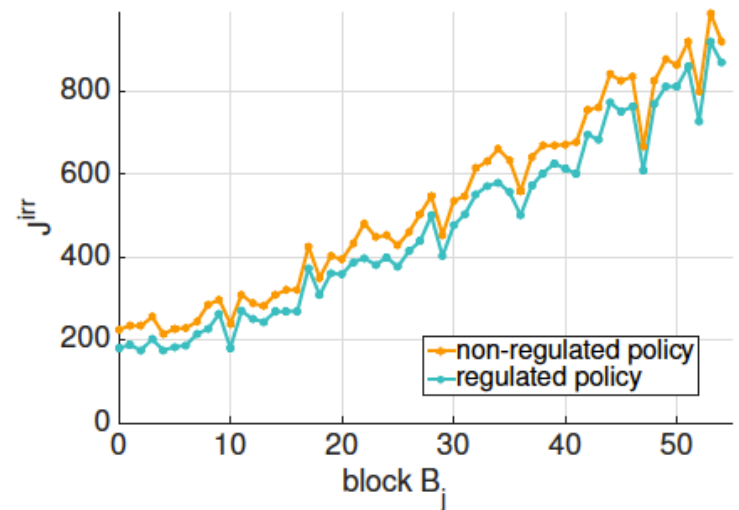


## Simulations: decreasing inflow (2)

Costs of the agents with the set-based protocol for inflow  $q_\tau$  with a decreasing mean  $\mu_q$



(a) city agent



(b) irr agent



# Conclusions

We propose a monotonic concession negotiation approach to model the interaction between agents that represent different interests in the management of water resources systems

The model is expressive and can naturally capture observed behaviors

## Future work

- Application to real data (ongoing)
- Investigation of theoretical properties, like the distance between initial proposals and final agreement



Thanks!

